

<b>Devi Ahilya University, Indore, India</b> <b>Institute of Engineering &amp; Technology</b>			<b>MSc – II Year (Applied Mathematics)</b> with Specialization in Computing & Informatics <b>Semester- IV</b>				
<b>Subject Code &amp; Name</b>	<b>Instructions</b> <b>Hours per Week</b>			<b>Credits</b>			
<b>AM4EM2: Mathematical Modelling</b>	<b>L</b>	<b>T</b>	<b>P</b>	<b>L</b>	<b>T</b>	<b>P</b>	<b>Total</b>
	<b>3</b>	<b>1</b>	<b>-</b>	<b>3</b>	<b>1</b>	<b>-</b>	<b>4</b>
<b>Duration of Theory Paper:</b> <b>3 Hours</b>							

### Learning Objectives:

- To provide rigorous instruction in fundamental mathematical concepts and skills presented in the context of real-world applications.
- Gain a working knowledge of core techniques behind mathematical modelling and develop a basic ability to quantify certain phenomena associated with the physical sciences.
- Represent real-world systems in a mathematical framework..

**Prerequisites:**Basics of algebra, differential equation, difference equations andgraphs.

## COURSE OF CONTENTS

### UNIT I

**Concept of models:** Types of models- Iconic, analogue and symbolic models, Classification of models, Meaning and formulation of mathematical models, example.

**Mathematical modeling through algebra:** Retail pricing model, Student assessment problems, Electricity tariff model, EOQ model for inventory control.

### UNIT II

**Mathematical Modelling through Ordinary Differential Equations of First order:** Linear Growth and Decay Models – Non-Linear Growth and Decay Models – Compartment Models – Dynamic problems – Geometrical problems. Population Dynamics – Epidemics – Compartment Models.Domar's macro model; Domar's debt model

### UNIT III

**Mathematical Modelling through Ordinary Differential Equations of Second Order:** Planetary Motions – Circular Motion and Motion of Satellites – Mathematical Modelling through Linear Differential Equations of Second Order – Miscellaneous Mathematical Models. Samuelson's capital Investment model, Philips stabilization model for closed economy.

### UNIT IV

**Mathematical Modelling through Difference Equations:** Simple Models – Basic Theory of Linear Difference Equations with Constant Coefficients – Economics and Finance – Population Dynamics and Genetics – Probability Theory. Models based on linear difference equations -Cobweb model, Harrod Domar growth model, Consumption model, Samuelson's multiplier- accelerator model.

### UNIT V

**Mathematical Modelling through Graphs:** Solutions that can be Modelled Through Graphs – Mathematical Modelling in Terms of Directed Graphs, Signed Graphs, Weighted Digraphs and Unoriented Graphs.

### Learning Outcomes:

Upon completing the course, students will be able to:

- To create mathematical models of empirical or theoretical phenomena in domains such as the physical, natural, or social science.

- Draw inferences from models using mathematical techniques including problem solving, quantitative reasoning, and exploration using multiple representations such as equations, tables, and graphs;
- Not only take an analytical approach to problems but also use computer programming and statistical analysis skills to efficiently model systems.

**BOOKS RECOMMENDED:**

[1] J.N. Kapur, Mathematical Modelling, New Age International, 1988.

[2] Martin Brann C.S Coleman, DA Drewc(Eds) differential equation models.

[3] C.L.Liu, Elements of Discrete Mathematics, McGraw-Hill Education, 2nd ed., 1986.

[4] Edward A. Bender, Introduction to Mathematical Modelling, Dover Publications, 1st ed., 2000.

[5] D.N. Burghes, A.D. Wood, Mathematical Models in the social, management, and life sciences, New York: Halsted Press, 1980.

[6] Zafar Ahsan, Differential Equations and Their Applications, 2<sup>nd</sup>Ed., Prentice-Hall of India Pvt. Ltd, 2004.

[7] Michael D Alder, An Introduction to Mathematical Modelling, HeavenForBooks.com, 2001.