

<b>Devi Ahilya University, Indore, India</b> <b>Institute of Engineering &amp; Technology</b>				<b>MSc – II Year (Applied Mathematics)</b> with Specialization in Computing & Informatics <b>Semester- IV</b>			
<b>Subject Code &amp; Name</b>	<b>Instructions</b> <b>Hours per Week</b>			<b>Credits</b>			
<b>AM4EM3: Number Theory/ Cryptography</b>	<b>L</b>	<b>T</b>	<b>P</b>	<b>L</b>	<b>T</b>	<b>P</b>	<b>Total</b>
<b>Duration of Theory Paper: 3 Hours</b>	<b>3</b>	<b>1</b>	<b>-</b>	<b>3</b>	<b>1</b>	<b>-</b>	<b>4</b>

### Learning Objectives:

- The course aims to give elementary ideas from number theory which will have applications in cryptology.
- Identify and apply various properties of and relating to the integers including the Well-Ordering Principle, primes, unique factorization, the division algorithm, understand the concept of a congruence,
- To impart the knowledge of encryption and decryption techniques and their applications in managing the security of data.

**Prerequisites:** Set theory, algebra of functions.

## COURSE OF CONTENTS

### UNIT I

Divisibility and Euclidean algorithm, congruences, applications to factoring.

### UNIT II

Finite fields, Legendre symbol and quadratic reciprocity, Jacobi symbol.

### UNIT III

Cryptosystems, diagraph transformations and enciphering matrices, Symmetric key cryptosystem, traditional techniques, Key range and size, Deffie-Hellman key exchange, various types of attacks, algorithm types and modes, various symmetric key algorithms (DES, IDEA, RC5, Blowfish)

### UNIT IV

Asymmetric key cryptography, concept, RSA algorithm, digital envelope, concept of message digest, MD5 algorithm, Authentication requirements, Digital signatures, message authentic codes, Knapsack algorithm.

### UNIT V

Primality and Factoring, Pseudoprimes, Carmichael number, Primality tests, Strong Pseudoprimes, Monte Carlo method, Fermat factorization, Factor base, Implication for RSA, Continued fraction method. Elliptic curves - basic facts, Elliptic curve cryptosystems.

### Learning Outcomes:

Upon completing the course, students will be able to:

- Solve problems in elementary number theory.
- Apply elementary number theory to cryptography.
- Develop a deeper conceptual understanding of the theoretical basis of number theory and identify how number theory is related to and used in cryptography.

### BOOKS RECOMMENDED:

- [1] Neal Koblitz, A Course in Number Theory and Cryptology, Graduate Texts in Mathematics, Springer, 1994.
- [2] Williams Stallings, Cryptography & Network Security, Pearson Education 3<sup>rd</sup> edition, 2004.
- [3] Atul Kahate, Cryptography & Network Security, Tata McGraw Hill, New Delhi, 2005.
- [4] Thomas Koshy, Elementary Number Theory with Applications, Academic Press, 2007.

